

Tejas Desai

A Multiple-Testing Approach to the Multivariate Behrens-Fisher Problem

with Simulations and
Examples in SAS®



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ISSN 2191-544X
ISBN 978-1-4614-6442-6
DOI 10.1007/978-1-4614-6443-3
Springer New York Heidelberg Dordrecht London

ISSN 2191-5458 (electronic)
ISBN 978-1-4614-6443-3 (eBook)

Library of Congress Control Number: 2013931259

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