

# {essentials{

Karim Ghaib

## Introduction to Computational Fluid Dynamics



Springer

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ISSN 2197-6708

essentials

ISBN 978-3-658-37621-5

<https://doi.org/10.1007/978-3-658-37619-2>

ISSN 2197-6716 (electronic)

ISBN 978-3-658-37619-2 (eBook)

This book is a translation of the original German edition „Einführung in die numerische Strömungsmechanik“ by Ghaib, Karim, published by Springer Fachmedien Wiesbaden GmbH in 2019. The translation was done with the help of artificial intelligence (machine translation by the service DeepL.com). A subsequent human revision was done primarily in terms of content, so that the book will read stylistically differently from a conventional translation. Springer Nature works continuously to further the development of tools for the production of books and on the related technologies to support the authors.

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## What You Can Find in This *essential*

- Mathematical basics of computational fluid dynamics
- A systematic description of the conservation equations for mass, momentum, and energy
- Most important models for the calculation of turbulence
- Most important methods for the discretization of the conservation equations
- Criteria for assessing the quality and fineness of computational meshes

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## Preface

The properties and effects of flows are important in many areas of science and engineering. Their prediction can be achieved by analytical, experimental, and numerical fluid mechanics. In this context, numerical fluid mechanics is becoming increasingly important. This is mainly due to the continuously increasing performance of computers. The currently available workstations are so powerful that calculation of complex flow problems is possible on them.

Users of computational fluid dynamics need to know a lot about the methods of this field. This *essential* provides an introduction to computational fluid dynamics. After an overview of mathematical basics, the conservation equations of fluid mechanics are formulated. Turbulence models are then explained. The main numerical methods are then described. Finally, types and evaluation criteria of computational meshes are given.

This book is recommended for both the beginner and the user in the field of computational fluid dynamics.

Zwingenberg, Germany

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